

# On the problem of non-zero word error rates for fixed-rate error correction codes in CV-QKD

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## Overview

The maximum operation range of continuous variable quantum key distribution systems is constrained by the efficiency of the forward error correction post-processing step. We show that the current definition of this forward error correction efficiency can exceed unity when employing fixed-rate error correction codes operating at high word error rates, which in turn would lead to achieving positive secret key over an entanglement breaking channel. We propose a new bound for the secure key rate equation and show new optimisation strategies for forward error correction codes.

## Background

Continuous variable quantum key distribution has been demonstrated for distances up to 100 km in optical fibers<sup>[1,2]</sup>. One of the main technological difficulty to achieve a positive key over large distances is to design Forward Error Correction (FEC) codes that achieve high efficiency at low Signal to Noise Ratio (SNR). The efficiency  $\beta$  of a FEC is defined as:

$$\beta_{\text{FEC}} = R / I_{\text{AB}}$$

Where  $I_{\text{AB}}$  is the theoretical channel capacity achievable for a given SNR, and  $R$  is the actual rate of the FEC code achieving perfect decoding for that SNR.

## LDPC — a First Pass

Multi Edge Low Density Parity Codes (ME-LDPC) can achieve high efficiency at low SNR<sup>[3]</sup>. In this regime, however, practical ME-LDPC codes exhibit a non zero Word Error Rate (WER), meaning they have a probability  $p_{\text{fail}}$  to fail to decode a codeword.

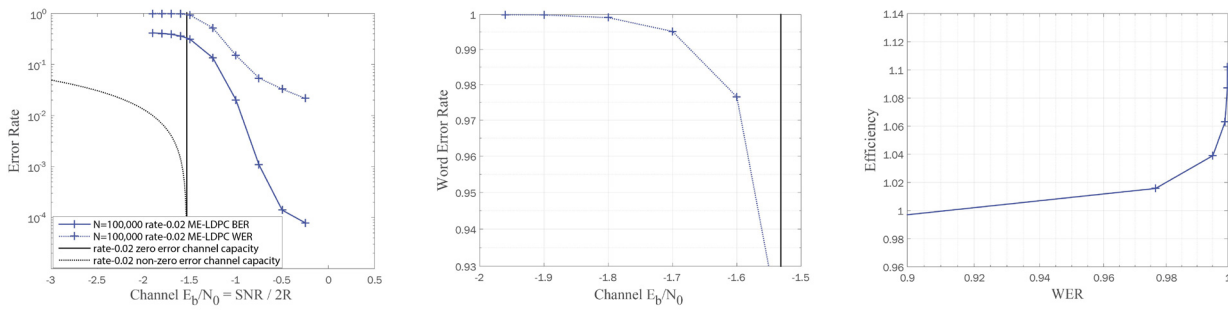
In order to take into account both the efficiency and WER of the ME-LDPC a new formulation of the key rate has been proposed<sup>[4]</sup>.

$$\Delta I = (\beta I_{\text{AB}} - I_{\text{E}}) (1 - p_{\text{fail}})$$

## LDPC — a Closer Look

The theoretical asymptotical (WER=0) efficiency of a ME-LDPC can be estimated using the density evolution formalism. In practice ME-LDPC decoders accept codewords of finite length and therefore can function with an efficiency greater than unity.

The following figures show the WER and efficiency of a rate 0.02 ME-LDPC working on a codeword of size N=100,000.



**The Issue**

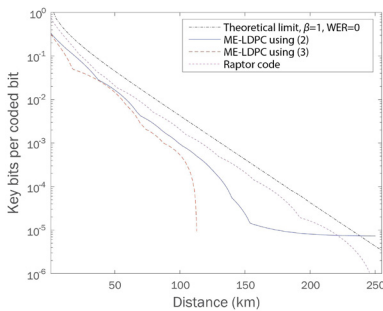
In the accepted formalism ME-LDPC codes working with an efficiency greater than unity allow establishment of a positive key over an entanglement breaking channel.

**Another Approach**

The non zero WER of the ME-LDPC can be interpreted as a post-selection step. A lower bound for the key rate can therefore be derived as follows:

$$\Delta I = (1 - p_{fail}) \beta I_{AB} - I_E$$

Although the previous bound is not tight, positive key rate can still be achieved. It is possible to keep using these ME-LDPC codes with a noticeable drop of performance only in the high loss regime. Alternatively rateless codes with zero WER such as the Raptor codes should be considered<sup>[6]</sup>.



**References**

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